

$$\int_0^2 x^2 dx$$

Write approximations to the integral for  $n$  subdivisions using left sums, right sums, midpoint sums and trapezoidal sums.

$$\int_{-3}^{-1} \left( x e^{x^2} \right) dx$$

**Arrange in order, smallest  
to largest**

**L20, T20, M20, R20**

$$\int_2^6 (\ln(x)) dx$$

Find  $L_{16}$  and  $M_{16}$  Estimate the error.

Are the approximations too big or too small?

How many terms are necessary for each to get the answer to within 0.0005?

$$\int_1^3 \left( \frac{1}{x} \right) dx$$

Write the summation to approximate this integral using left sums, right sums, trapezoids and midpoints. In each case use 400 subintervals and estimate your error.

$$\int_{-2}^2 \left( e^{x^2} \right) dx$$

Write the summation to approximate this integral using left sums, right sums, trapezoids and midpoints. In each case use 400 subintervals and estimate your error.

$$\frac{dy}{dx} = x - y$$

Determine  $y$  using Euler's method and 5 increments of 0.1 starting from  $(1,0)$  . Repeat the process starting from  $(2,0)$  Show steps

$$\frac{dy}{dx} = x + y$$

Determine  $y$  using Euler's method and 5 increments of 0.1 starting from  $(1,0)$  . Repeat the process starting from  $(2,2)$  Show steps

$$\frac{dy}{dx} = x^2 + y^2$$

Estimate a solution to this differential equation using Euler's method and four steps, starting at (0,0) and ending at x=4.

Then do it using 8 steps



Approximate  $\int_1^9 \left( \frac{100}{(x+1)^2} \right) dx$

using Simpson's rule and 32 subintervals. Estimate your error.

Find the area of the region between these two curves

$$y = 12 - x^2$$

$$y = 2x^2$$

Find the area of the region between these two curves

$$y = 2x^2 - 10$$

$$y = x$$